

## Pump control

### Aim of the work

To understand the components of the process.

### 1 Pump

With ARMSTRONG 4380 water pump the system pressure is kept  $80 \text{ kPa}$  where water consumption varies between  $(10..50) \text{ L/s}$ . [Curved arrow in the figure is not included into the task].

Pump speed  $n = (0 - 1500) \text{ r/min}$  controlled by a linear frequency converter with control signal  $u = 0 \dots 100\%$ .

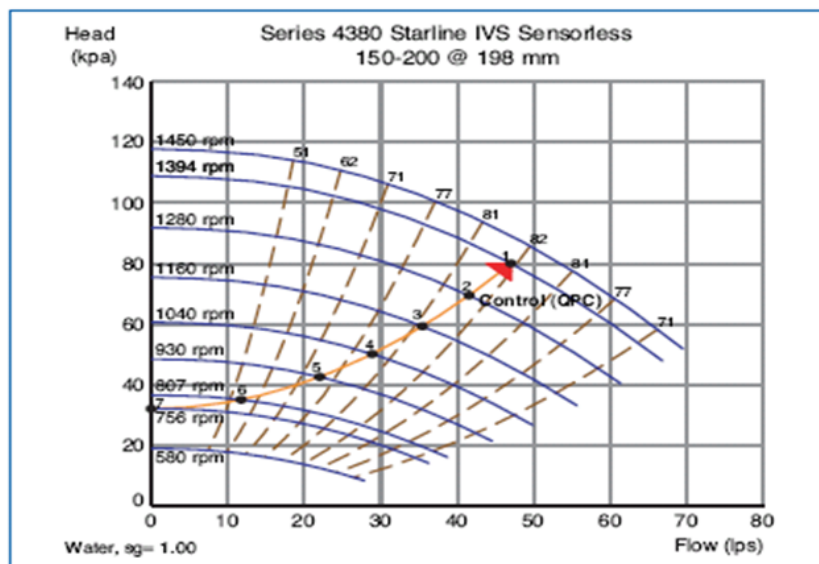


Figure 1: ARMSTRONG 4380 water pump

### Work flow

1. Calculate coefficients  $k_1$  and  $k_2$  from the equation  $p(q, n) = k_1 \cdot n^2 - k_2 \cdot q^2$  with rotation speed  $n = 1450 \text{ r/min}$ .
2. Do these parameters describe other pump speeds?
  - (a) Calculate in Excel the pump equation  $p(q, n)$  values as a function of  $q = 0, 10, 20, \dots, 80 \text{ l/s}$  (Line), with the parameters  $n = 1450, 1394, \dots$  (Column)

(b) Provide data by figure;

Place one on the other: task's and Excel figures,

Assess the match,

Adjust the parameters  $k_1, k_2$ .

3. Pressure  $p$  control  $p = p_0$  by rotation speed  $n$  due to consumption  $q$  changes.

(a) Determine the control signal  $u$  range.  $n = F_1(p_0, q)$ ,  $n$ -range  $n_{\max} \dots n_{\min}$ ,

(b) What is the block (frequency converter + pump) gain  $K$  value and its range? Gain

$$K_p = \frac{dp}{dn}.$$

## Comments

### 2 Industrial pumps

Most liquids are moved by industrial pumps. Pumping costs consist of

- 5% of capital expenditures,
- 10 – 15% of exploitation,
- 85% of the energy cost ( $\approx 100\times$  more than the price!)

Industrial pumps use 20% of the power generated (paper, chemical and petrochemical industries, up to 30...50%).

Pumps with higher efficiency (with frequency converters) are 60 – 80%, this characteristic significantly affects the cost.

View:

<http://www.PumpLearning.org>,

<http://www.pump-zone.com>,

<http://www.pumps.org>,

<http://www.engineeringtoolbox.com>.

<http://www.pumpsystemsmatter.org>,

### Where does the energy go during the pumping?

1. Potential energy

- Pressurized liquid  $p$ , rises on the height  $h$ ;
- Work  $E_p = mg \cdot h = V\rho gh = Vp$  [J], where  $V$  - volume,  $p$  - pressure,  $q$ -consumption;
- Power  $P_p = \frac{dE_p}{dt} = qp$  [W]

## 2. Kinetic energy

- Energy  $E_k = mv^2/2$  [J], where  $v$  - fluid velocity [m/s];
- Power  $P_k = qv^2/2$  [W] during the pumping *pot.energy*  $\rightarrow$  *kin. energy*!

3. Losses ( due to change in flow rate and direction)  $\sim 10\%$ .

## 3 Pump characteristics

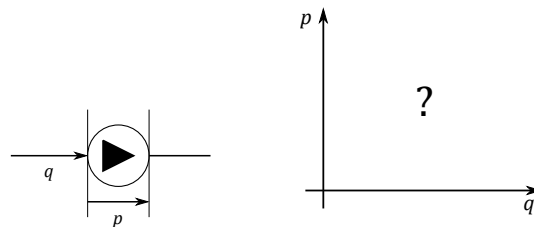


Figure 2: Pressure-consumption dependency

- Ideal pump  $p = p_{\max}$

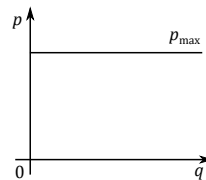


Figure 3: Ideal pump characteristic

- Fluid flow  $\Delta p \sim q^2$ ,  $\Delta p = k \cdot q^2$  turbulent

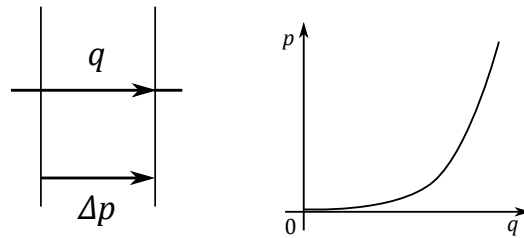


Figure 4: Turbulent flow

- Real pump—centrifugal pump; internal resistance: Opening  $S [m^2]$  impeller

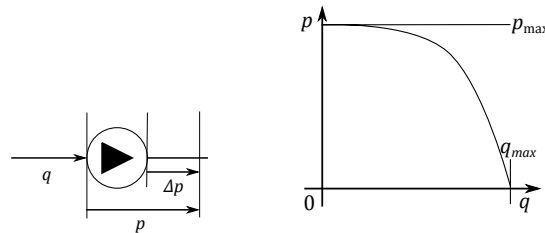


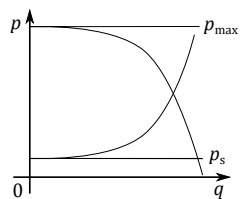
Figure 5: Centrifugal pump

- $p = p_{\max} - \Delta p$ ;  $F(p, q) = 0$ ; analogy with an electric battery, but nonlinear
- maximum flow  $q_{\max}$

$$p = p_{\max}[1 - (q/q_{\max})^2]$$

- Is it a maximum performance too? Pump curve  $F(p, q) = 0$  is represented by two parameters.

- Real pump + external resistance (load)



Operating point  $(p, q)$ , the pump characteristic is designated by the load and changes due to the load change.

- Variable rotational speed  $n$ ,  $p_{\max} \sim n^2$  parameters:

$$F(p, q, n) = 0, \quad p = k_1 \cdot n^2 - k_2 \cdot q^2 \quad (k_1, k_2) \quad (1)$$

$$p = \dots (n/n_o)^2 \quad (\dots n_o)$$

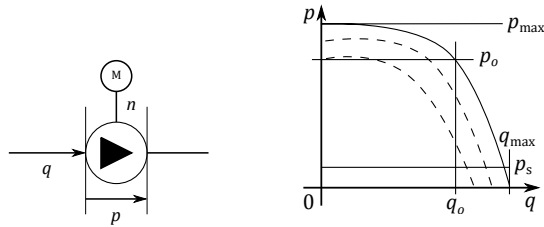


Figure 6: Variable rotational speed