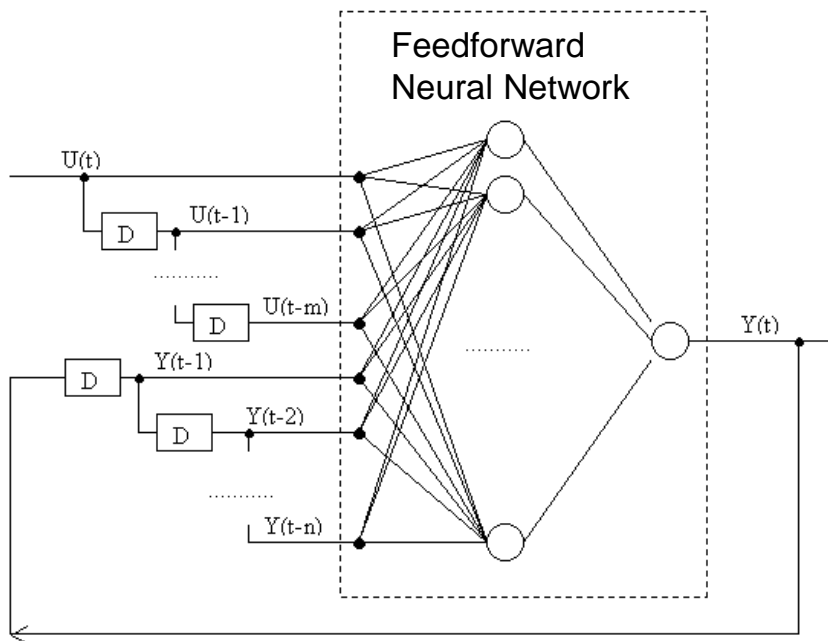




# Neural Networks based control of nonlinear systems

## Identification of dynamic systems with Artificial Neural Networks

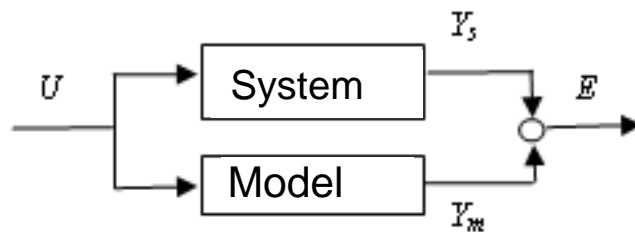
Dynamic/ feedback network:



$$y(t) = F_2 \cdot (W_2 \cdot (F_1 \cdot (W_1 \cdot \begin{bmatrix} u(t) \\ \vdots \\ u(t-m) \\ y(t-1) \\ \vdots \\ y(t-n) \end{bmatrix} + \Theta_1) + \Theta_2) =$$

$$= f_{nn}(u(t), \dots, u(t-m), y(t-1), \dots, y(t-n))$$

## Identification with Artificial Neural Networks



$$E = Y_s - Y_m$$

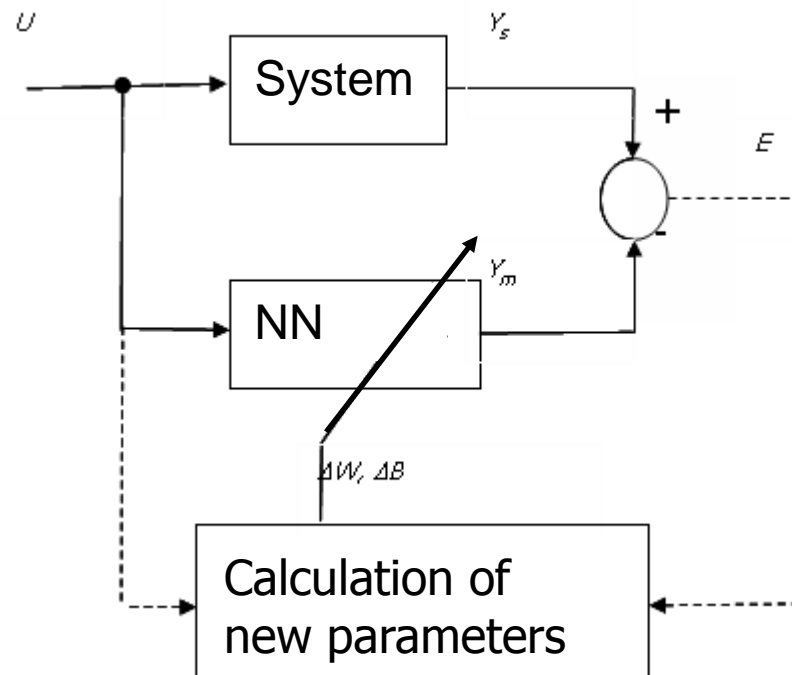
$$E \rightarrow 0$$

$U$  is the input of the system and the model

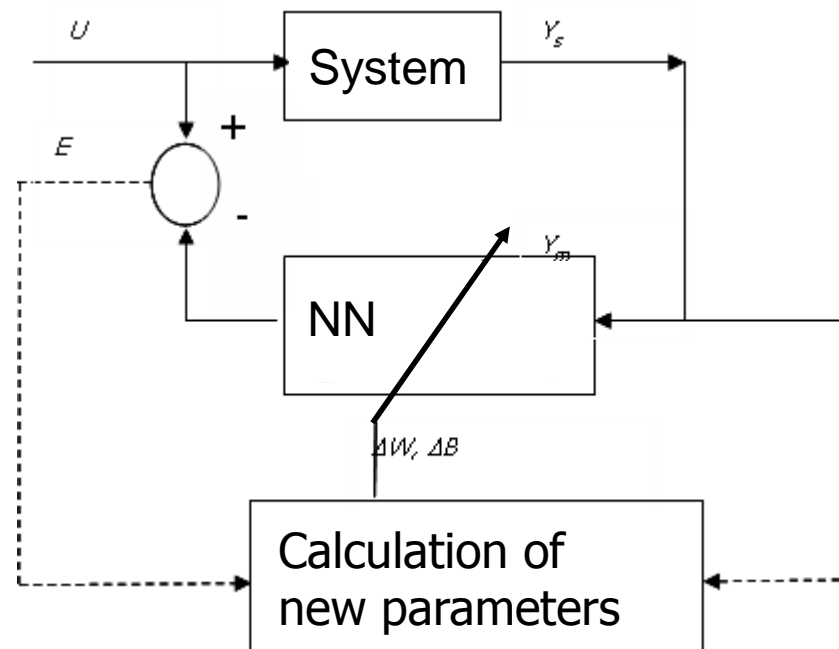
$Y_s$  is the output of the system

$Y_m$  is the output of the model

## Identification with Artificial Neural Networks



## Inverse model





## Inverse model

---

$$f^{-1} : Y(t) \rightarrow U(t-1)$$

$$U(t-1) = f^{-1}(Y(t), \dots, Y(t-q), U(t-2), \dots, U(t-r))$$

Consider a system:  $y(t) = f^{-1}(y(t-1), y(t-2), u(t-1), u(t-2))$

$$u(t-1) = f^{-1}(y(t), y(t-1), y(t-2), u(t-2))$$

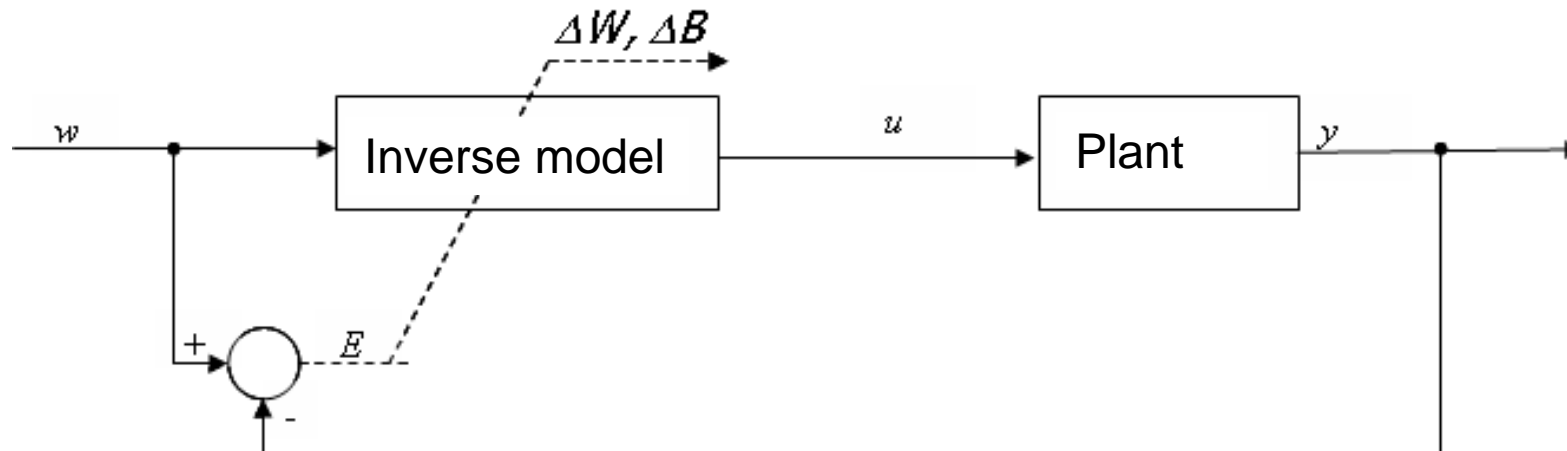
## Inverse model based control



$$u(t-1) = f^{-1}(y(t), y(t-1), y(t-2), u(t-2))$$

Here  $y(t) = w(t)$

# Inverse model based adaptive control



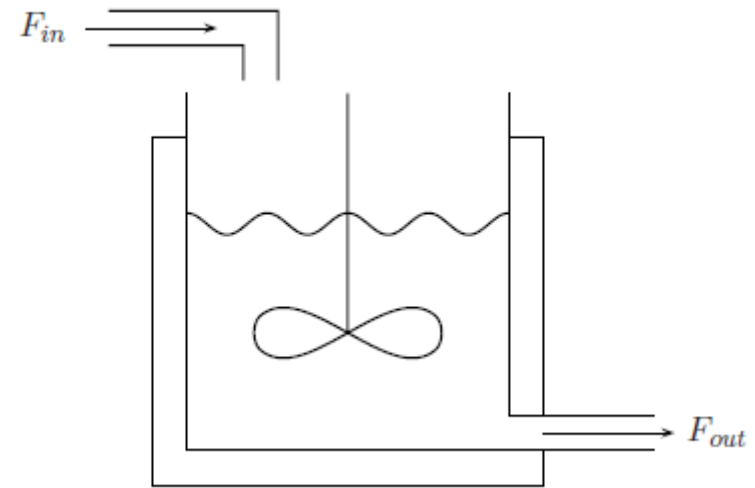
$$E \rightarrow 0$$



## Example: Jacketed CSTR (Continuous Stirred Tank Reactor)

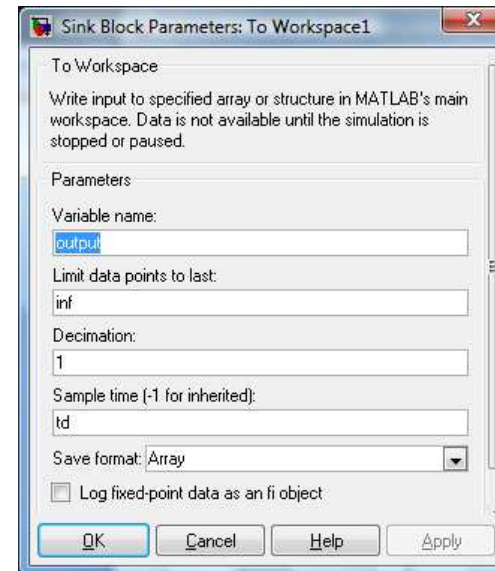
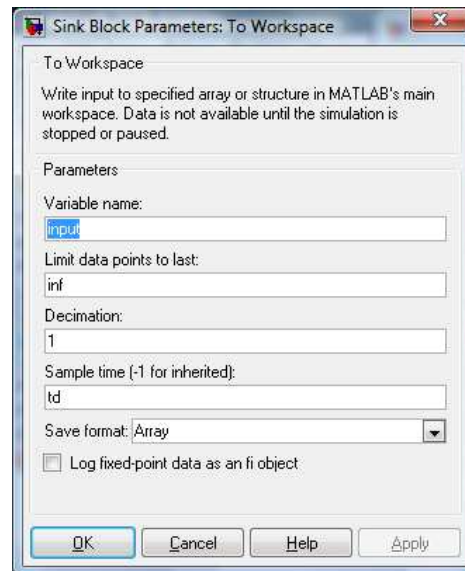
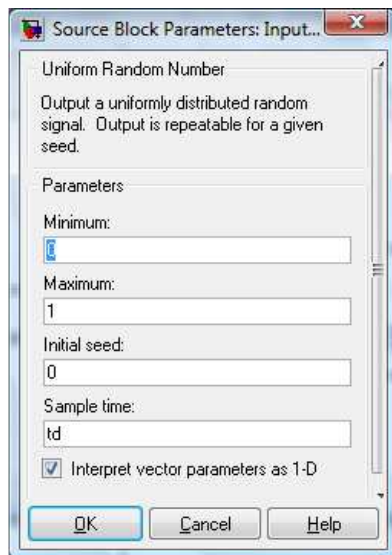
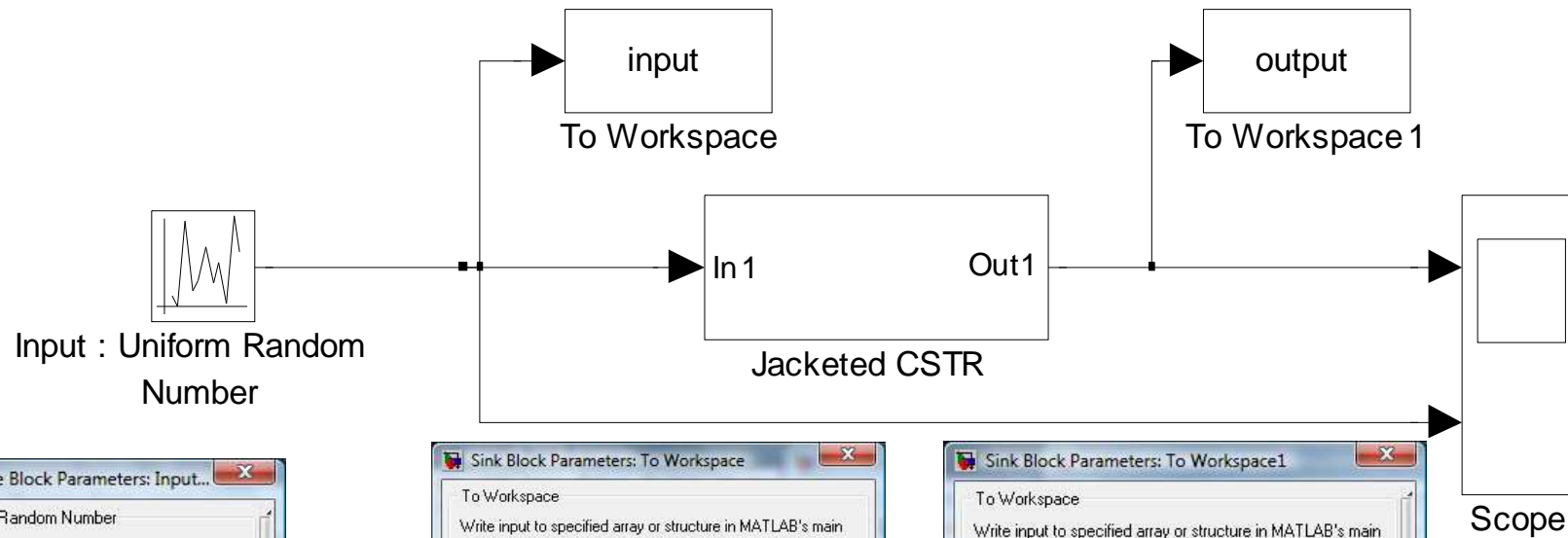
Input-Output equation:

$$\begin{aligned} y(t+2) = & 0.7653y(t+1) - 0.231y(t) + \\ & + 0.4801u(t+1) - 0.6407y^2(t+1) + \\ & + 1.014y(t)y(t+1) - 0.3921y^2(t+1) + \\ & + 0.592y(t+1)u(t+1) - 0.5611y(t)u(t+1) \end{aligned}$$





## Collecting input-output data



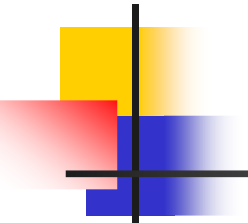


## Training of inverse model

---

```
td=1
N=size(output,1)
P=[output(3:N)';output(2:N-1)';output(1:N-2)']
T=input(2:N-1)'
global net_c

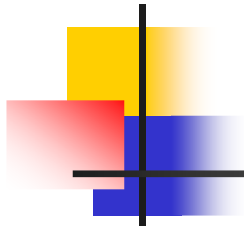
net_c=newff([0 1; 0 1; 0 1],[5 1],{'tansig','purelin'})
net_c.trainParam.show=1;
net_c.trainFcn='traingd';
net_c.trainParam.epochs=3000;
net_c=train(net_c,P,T)
```



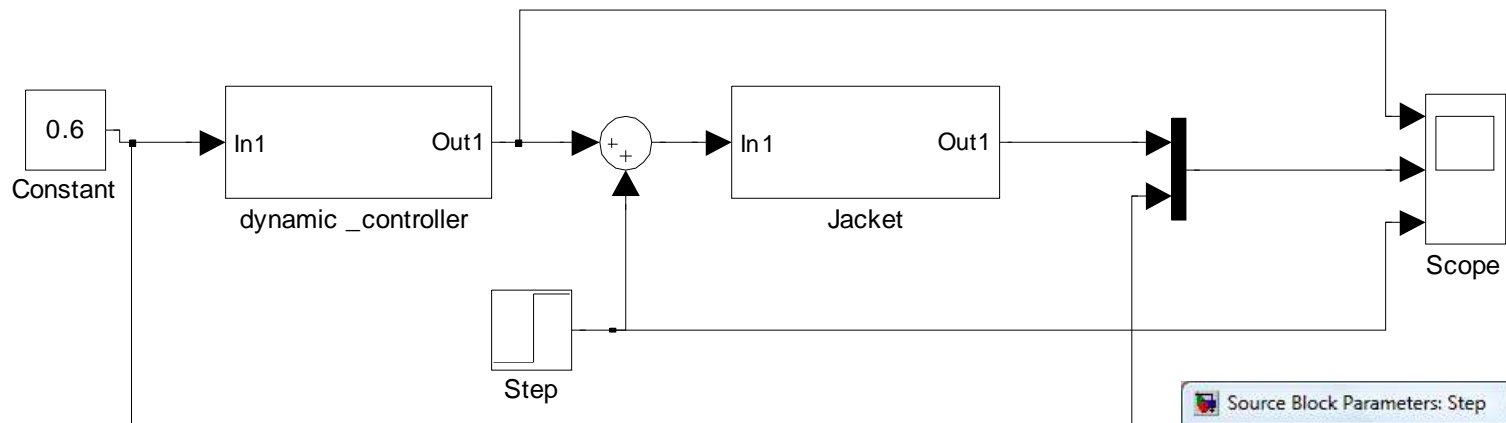
## Implementation of the controller in MATLAB (m-file controller.m)

---

```
function control=controller(u)
global net_c
control=sim(net_c,u);
```



# Control scheme



Source Block Parameters: Step

Step

Output a step.

Parameters

Step time: 15

Initial value: 0

Final value: 0.2

Sample time: 0

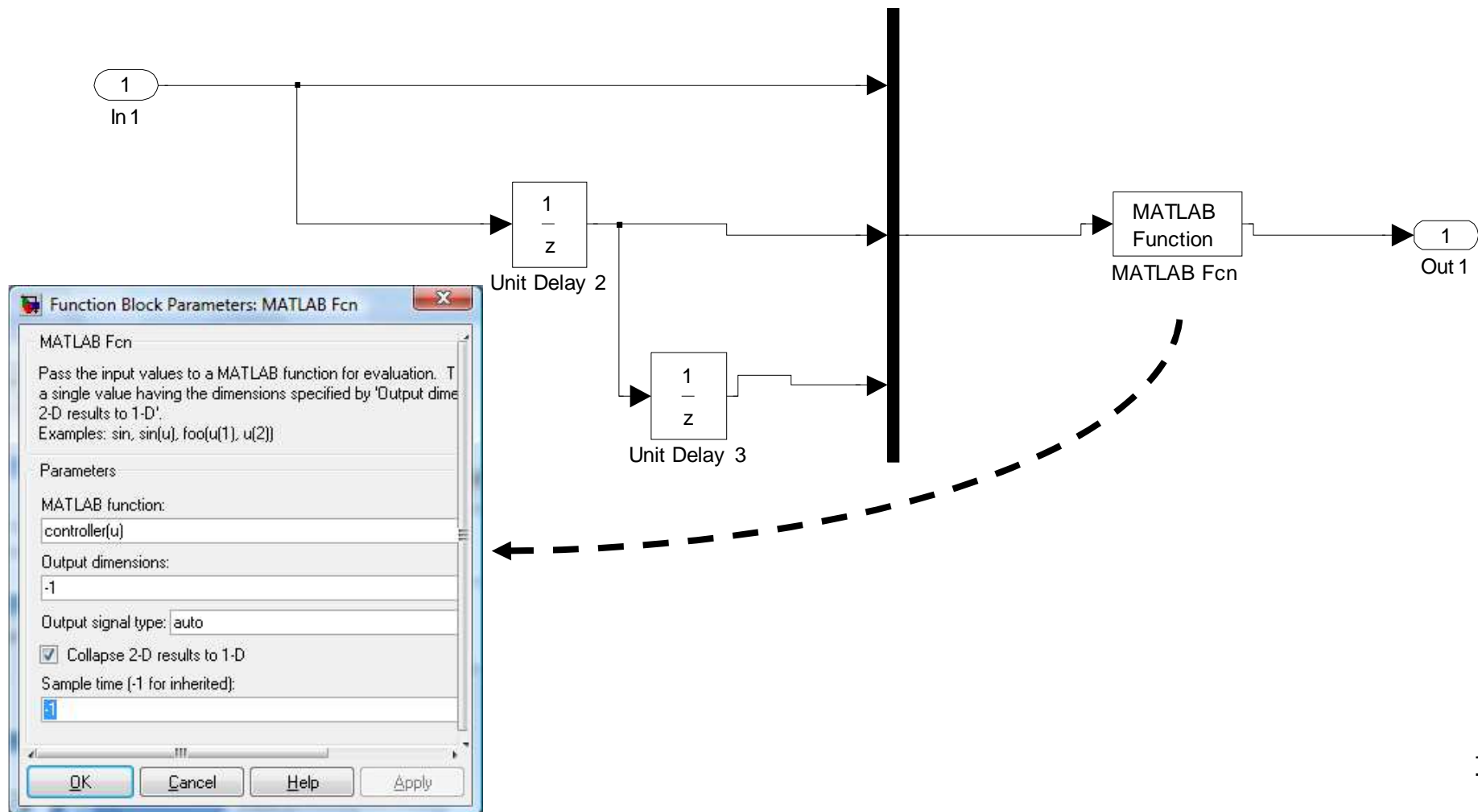
Interpret vector parameters as 1-D

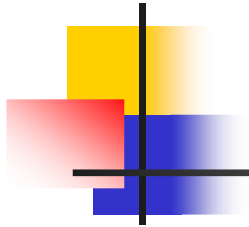
Enable zero crossing detection

OK Cancel Help

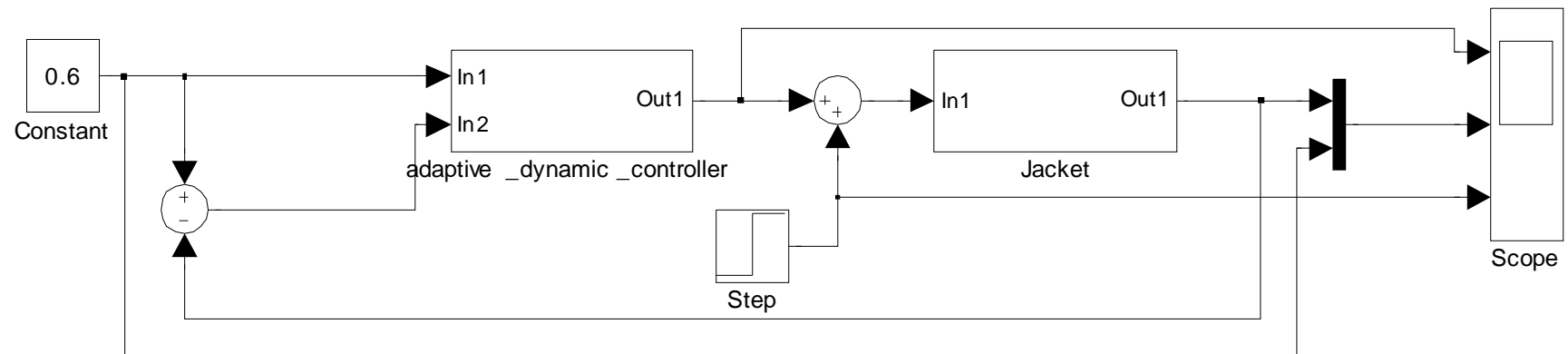


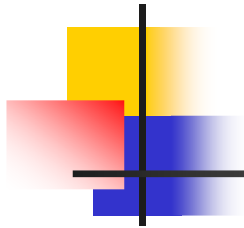
## "dynamic\_controller" block



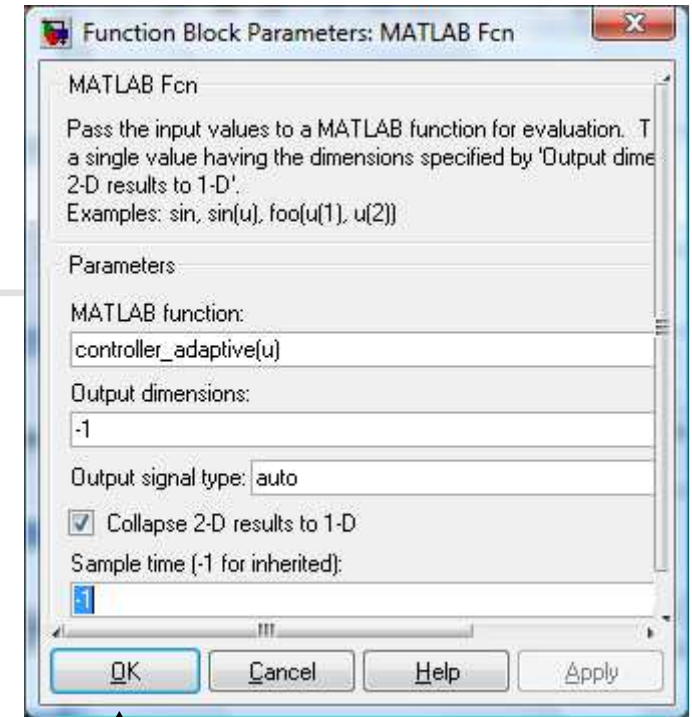
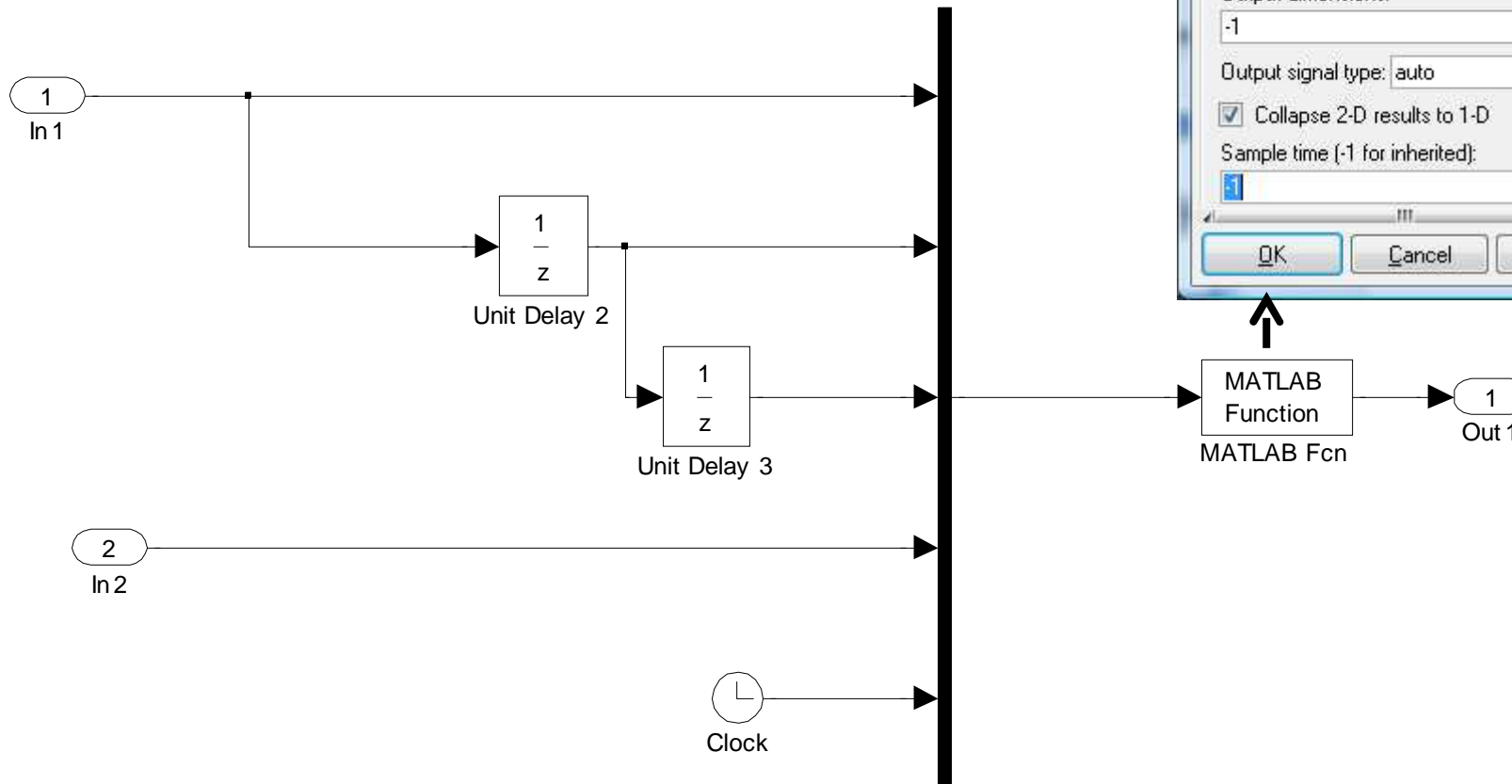


# Adaptive control scheme





## "adaptive\_dynamic\_controller" block







Adaptive controller = function  
"controller\_adaptive" (m-file controller\_adaptive.m)

---

```
function control=controller_adaptive(u)
global net_c
inp=u(1:3);
error=u(4);
time=u(5);
control=sim(net_c,inp);
if time>10
net_c=adapt(net_c,inp,control+error);
end
```