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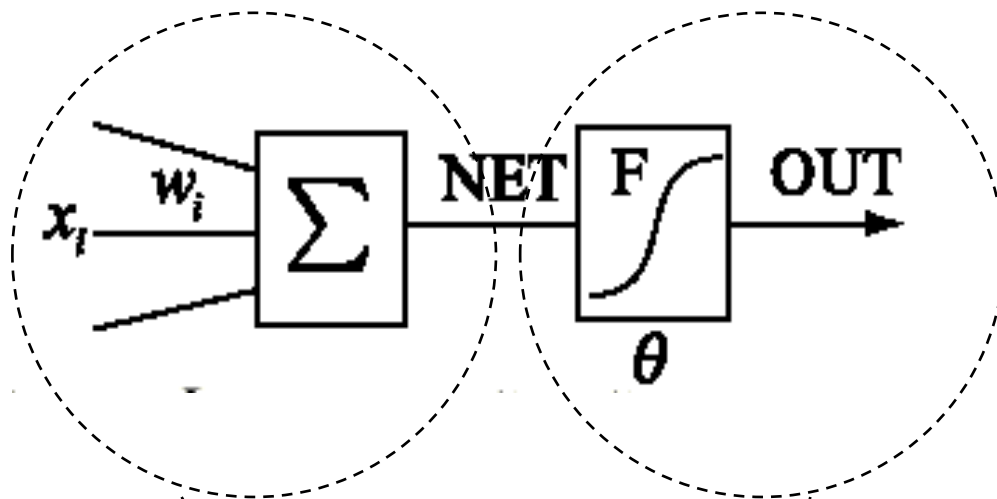
*Modelleerimine ja Juhtimine  
Tehisnärvivõrgudega*

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*Identification and Control with  
artificial neural networks*

*Eduard Petlenkov,*

## Artificial neuron



Weighted sum

Nonlinear element

Input vector:  $X = \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix}$

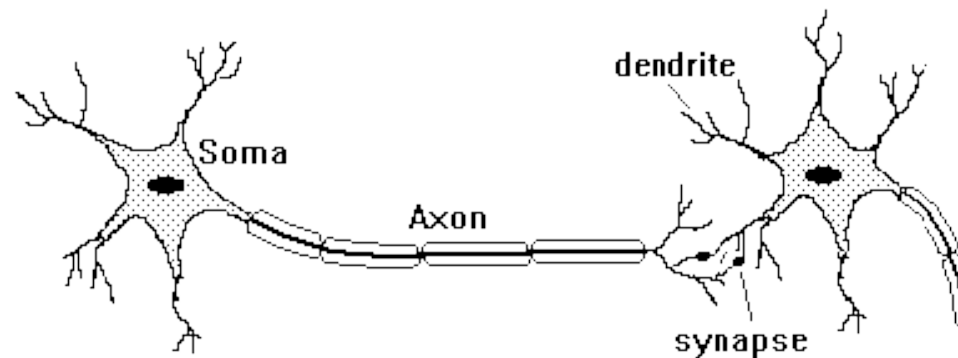
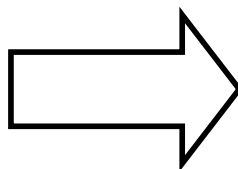
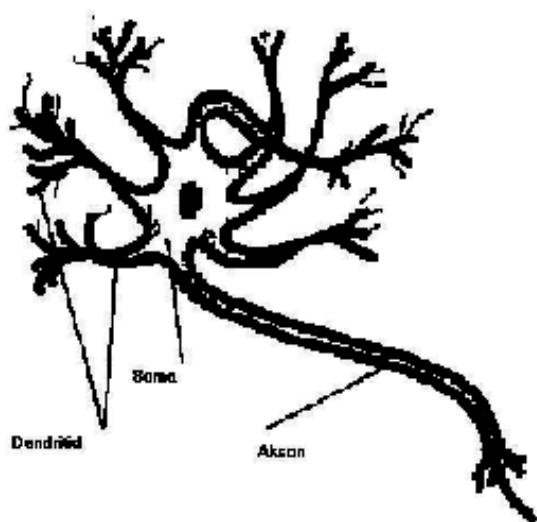
Vector of weight coefficients:

$$W = [w_1 \dots w_n]$$

Weighted sum:

$$NET = W \cdot X = [w_1 \dots w_n] \cdot \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix} = w_1 x_1 + \dots + w_n x_n$$

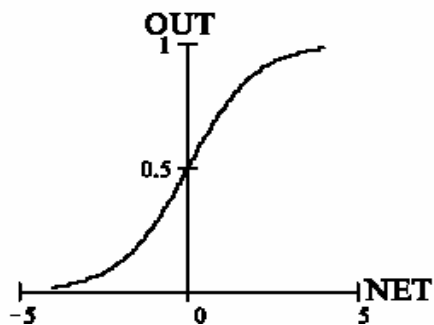
## Biological neuron and biological neural networks



## Activation functions (1)

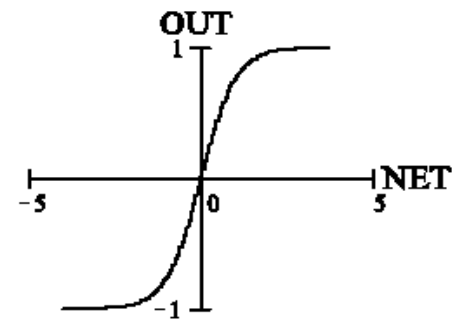
$$OUT = f(NET)$$

Sigmoid functions are having an "S" shape (**sigmoid curve**)



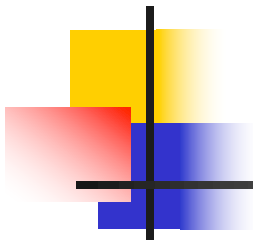
1 Logistic function

$$OUT = \frac{1}{1 + e^{-NET}}$$

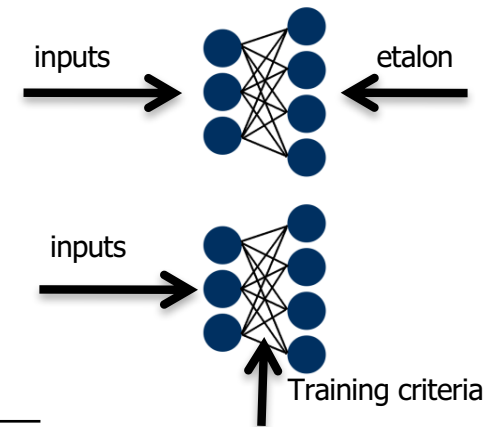
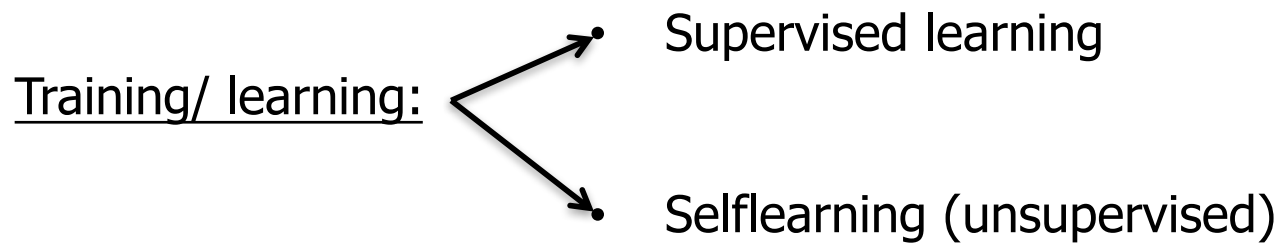
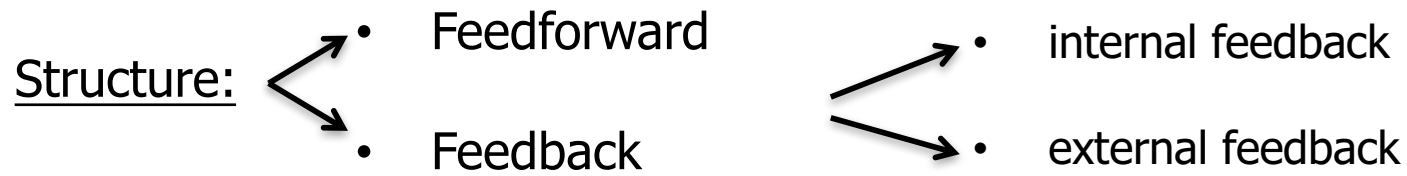


2 Hyperbolic tangent

$$OUT = \frac{e^{NET} - e^{-NET}}{e^{NET} + e^{-NET}}$$



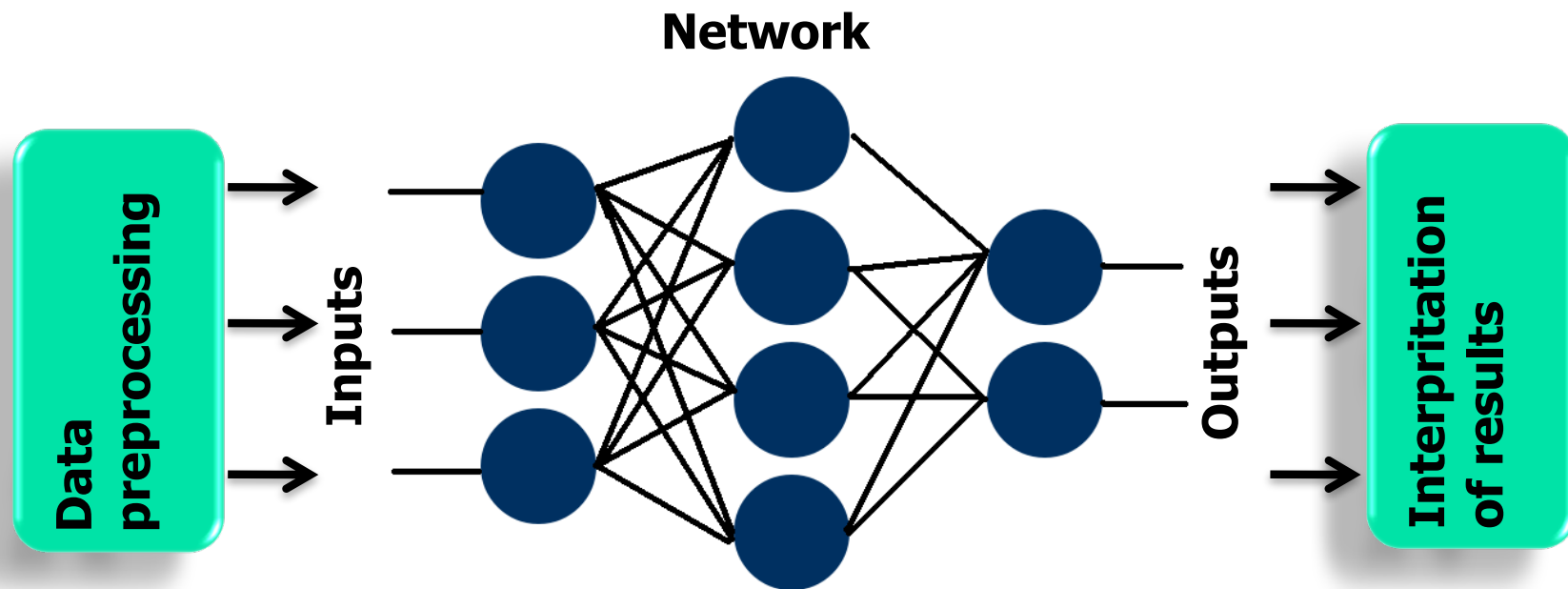
## Types of artificial neural networks





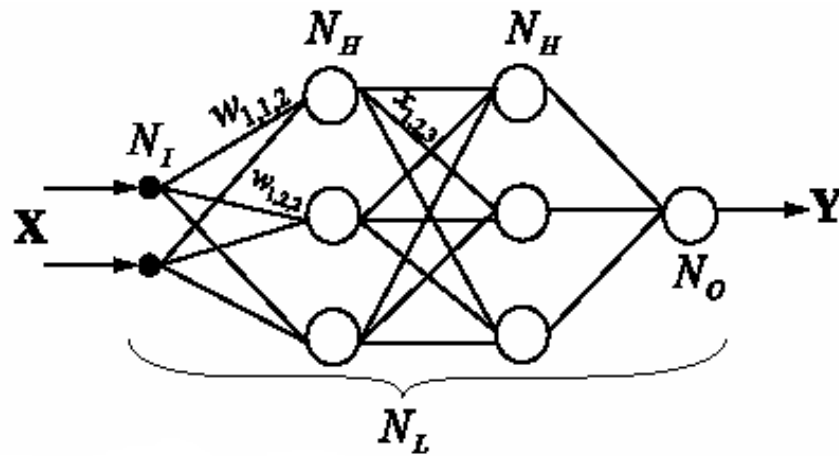
## How to use artificial neural networks

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## Feedforward neural networks and multilayer perceptron

Feedforward networks are networks in which an output of a neuron can be connected only with an input of a next layer neuron.



*“from each to each”*

$N_I$  - Input layer

$N_O$  - Output layer

$N_H$  - Hidden layer

$w_{ijl}$  - Weighting coefficients, where

$i$  is the number of the neuron's input

$j$  - neuron's number in the layer

$l$  - number of the layer



## Mathematical function of a two-layer perceptron

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$$X = \begin{bmatrix} x_1 \\ \vdots \\ x_n \end{bmatrix}; \quad Y = \begin{bmatrix} y_1 \\ \vdots \\ y_m \end{bmatrix}; \quad W_1 = \begin{bmatrix} w_{111} & \cdots & w_{n11} \\ \vdots & \ddots & \vdots \\ w_{1k1} & \cdots & w_{nk1} \end{bmatrix}; \quad \Theta_1 = \begin{bmatrix} \theta_{11} \\ \vdots \\ \theta_{k1} \end{bmatrix};$$

$$W_2 = \begin{bmatrix} w_{112} & \cdots & w_{k12} \\ \vdots & \ddots & \vdots \\ w_{1m2} & \cdots & w_{km2} \end{bmatrix}; \quad \Theta_2 = \begin{bmatrix} \theta_{12} \\ \vdots \\ \theta_{m2} \end{bmatrix};$$

$F_1$  - Activation function of the hidden layer neurons;

$F_2$  - Activation function of the output layer neurons.

$$Y = F_2(W_2(\underbrace{F_1(W_1X - \Theta_1)}_{\text{output of the first layer}}) - \Theta_2)$$

$\underbrace{\hspace{15em}}_{\text{output of the network}}$